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The following information is a python code script which can be used to replicate the findings.

- # Natasha Rozario
- # This script reads data from an excel file about past procedures and the times they took, and uses google's or-tools
- # to calculate scheduling times for each procedure type that minimizes the undertime and overtime frequencies of
- # the operating room as a whole

```
from __future__ import print_function
from ortools.sat.python import cp_model
import pandas as pd
import sys
import math
```

#

```
# Parameters
targetOvertimeFrequency = 0.2
targetUndertimeFrequency = 0
undertimeCostWeight = 1
overtimeCostWeight = 1
```

```
arguments = sys.argv
excelInputFile = 'input.xlsx'
excelOutputFile = 'output.xlsx'
```

dfP = dfP.iloc[:, :].values.tolist() dfP = [x for y in dfP for x in y]

overtimeBlockLength = 15 # length of overtime blocks in minutes noOfNursesPerBlock = 2.5 # number of nurses per overtime block overtimeSalary = 75 # pay by block for overtime nurses

```
# Optional: get excel filenames from command line argument
if (len(arguments) > 1):
    excelInputFile = str(arguments[1])
    excelOutputFile = str(arguments[2])
# Read data from an excel file
```

```
data = pd.read_excel(r'' + excelInputFile, header=4)
# -----
# Input data from excel sheet columns
dfP = pd.DataFrame(data, columns=["Procedure"])
```

```
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dfD = pd.DataFrame(data, columns=["Date"])
dfD = dfD.get values()
dfD = [x for y in dfD for x in y]
dfE = pd.DataFrame(data, columns=["Book Dur"])
dfE = dfE.ilocl: :1.values.tolist()
dfE = [x for y in dfE for x in y]
dfA = pd.DataFrame(data, columns=["Actual Dur"])
dfA = dfA.iloc[:, :].values.tolist()
dfA = [x for y in dfA for x in y]
rawProcedures = [] # a list of each procedure performed
procedureTypes = [] # a list of all the procedure codes
rawDays = [] # a list of dates for each procedure performed
days = [] # a list of the dates in the data
rawExpectedTimes = [] # a list of scheduled times for each procedure performed
rawActualTimes = [] # a list of actual times for each procedure performed
# Input data into arrays
for i in range(len(dfE)):
  if str(dfE[i]) != 'nan':
    if dfD[i] not in days:
       days.append(dfD[i])
    rawExpectedTimes.append(dfE[i])
    rawDays.append(dfD[i])
    rawActualTimes.append(dfA[i])
    rawProcedures.append(dfP[i])
    if dfP[i] not in procedureTypes:
       procedureTypes.append(dfP[i])
procedureTypes.sort() # sort procedure types alphabetically
proceduresPerDay = {w: [] for w in days} # a map from a day to a list of procedures
performed on that day
for i in range(len(rawDays)):
  proceduresPerDay[rawDays[i]].append(rawProcedures[i])
expectedTimes = {w: [] for w in days} # a map from a day to a list of booking times for that
day
for i in range(len(rawDays)):
  expectedTimes[rawDays[i]].append(rawExpectedTimes[i])
actualTimes = {w: [] for w in days} # a map from a day to a list of actual procedure times for
that day
for i in range(len(rawDays)):
```

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count = len(days) # number of days

```
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  actualTimes[rawDays[i]].append(rawActualTimes[i])
# Pre-processing
originalBookTimes = {p: 0 for p in procedureTypes} # a map with average booking times for
each procedue
for p in procedureTypes:
  counter = 0
  for i in range(len(rawDays)):
    if p == rawProcedures[i]:
       counter += 1
       originalBookTimes[p] += rawExpectedTimes[i]
  originalBookTimes[p] = int(originalBookTimes[p] / counter)
expectedTotalTime = {} # a map from a day to the sum of booking times for that day
for day in days:
  expectedTotalTime[day] = 0
  for time in expectedTimes[day]:
    expectedTotalTime[day] += time
actualTotalTime = {} # a map from a day to the sum of actual procedure times for that day
for day in days:
  actualTotalTime[day] = 0
  for time in actualTimes[day]:
    actualTotalTime[day] += time
currentOvertimeCount = 0 # counts how many days the room went overtime
currentUndertimeCount = 0 # counts how many days the room went undertime
for day in days:
  if expectedTotalTime[day] + 0 < actualTotalTime[day]:
    currentOvertimeCount += 1
  elif actualTotalTime[day] + 15 < expectedTotalTime[day]:
    currentUndertimeCount += 1
minProcedureTime = {p: 1440 for p in procedureTypes} # a map from a procedure to its
minimum case time
maxProcedureTime = {p: 0 for p in procedureTypes} # a map from a procedure to its
maximum case time
for i in range(len(rawDays)):
  if rawActualTimes[i] < minProcedureTime[rawProcedures[i]]:
    minProcedureTime[rawProcedures[i]] = rawActualTimes[i]
  if rawActualTimes[i] > maxProcedureTime[rawProcedures[i]]:
    maxProcedureTime[rawProcedures[i]] = rawActualTimes[i]
```

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```
#
# Model
print("Starting model optimisation", file=sys.stderr)
# Decision variables
model = cp_model.CpModel() # Create the model
procedureSchedulingTimes = {} # Create a decision variable for the scheduling time of each
procedure type
for p in procedureTypes:
  procedureSchedulingTimes[p] = model.NewIntVar(int(minProcedureTime[p]),
int(maxProcedureTime[p]).
                              "procedureSchedulingTime" + str(p))
totalScheduledTime = {} # The total time scheduled for each day
overtimeTriggers = {} # Set to 1 if overtime for each day
undertimeTriggers = {} # Set to 1 if undertime for each day
for day in days:
  totalScheduledTime[day] = model.NewIntVar(0, 1000, "day" + str(day))
  overtimeTriggers[day] = model.NewIntVar(0, 1, "overtimeTrigger" + str(day))
  undertimeTriggers[day] = model.NewIntVar(0, 1, "undertimeTrigger" + str(day))
overtimeCount = model.NewIntVar(0, 1000, "overtimeCount") # Number of days that went
overtime
undertimeCount = model.NewIntVar(0, 1000, "undertimeCount") # Number of days that went
undertime
overtimeCost = model.NewIntVar(-1000, 1000, "overtimeCost") # Overtime cost
undertimeCost = model.NewIntVar(-1000, 1000, "undertimeCost") # Undertime cost
absOvertimeCost = model.NewIntVar(0, 100, "absOvertimeCost") # |overtime cost|
absUndertimeCost = model.NewIntVar(0, 100, "absUndertimeCost") # |undertime cost|
finalCost = model.NewIntVar(0, 100, "finalCost") # final cost is sum of overtime and
undertime costs
# Constraints
for day in days:
  # set totalScheduledTime to the sum of scheduled time in a day
  model.Add(totalScheduledTime[day] == (sum(procedureSchedulingTimes[i] for i in
proceduresPerDay[day])))
  # set overtime trigger to 1 if overtime
```

model.Add(1000 * overtimeTriggers[day] >= int(actualTotalTime[day]) -

totalScheduledTime[dav] - 0 - 1)

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```
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  # set overime trigger to 0 if not overtime
  model.Add(1500 * (1 - overtimeTriggers[day]) >= totalScheduledTime[day] -
int(actualTotalTime[day]) + 0)
  # set undertime trigger to 1 if undertime
  model.Add(1000 * undertimeTriggers[day] >= totalScheduledTime[day] - 15 -
int(actualTotalTime[day]) - 1)
  # set undertime trigger to 0 if not undertime
  model.Add(1000 * (1 - undertimeTriggers[day]) >= int(actualTotalTime[day]) -
totalScheduledTime[day] + 15)
model.Add(overtimeCount == (sum(overtimeTriggers[day] for day in days))) # count how
many days went overtime
model.Add(undertimeCount == (sum(undertimeTriggers[day] for day in days))) # count how
many days went undertime
model.Add((overtimeCost == overtimeCount - int(count * targetOvertimeFrequency))) #
calculate overtime cost
model.Add((undertimeCost == undertimeCount - int(count * targetUndertimeFrequency))) #
calculate undertime cost
# calculate absolute value of overtime cost
model.AddAbsEquality(absOvertimeCost, int(overtimeCostWeight) * overtimeCost)
# calculate absolute value of undertime cost
model.AddAbsEquality(absUndertimeCost, int(undertimeCostWeight) * undertimeCost)
model.Add((finalCost == overtimeCost + undertimeCost)) # calculate final cost
model.Minimize(finalCost) # Objective is to minimize final cost
solver = cp_model.CpSolver()
print("Starting to solve", file=sys.stderr)
status = solver.Solve(model)
______
# Print output to console and excel sheet
if status == cp_model.OPTIMAL or status == cp_model.FEASIBLE:
  print("Success!")
  rows = ["Number of days", "Number of cases", "Original overtime frequency", "Original
undertime frequency", "Model overtime frequency",
       "Model undertime frequency", "Model cases achieved", "Original Overtime Minutes
Used", "Model Overtime Minutes Used",
       "Original Overtime Cost", "Model Overtime Cost", "Original OR minutes used", "Model
OR minutes used", "", "Procedure Type"] + procedureTypes
```

dashboard = pd.DataFrame(index=rows,

```
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                 columns=["A", "B", "C", ])
  for r in rows:
    dashboard.at[r, "A"] = r
  # Output basic stats
  dashboard.at["", ""] = ""
  dashboard.at["Number of days", "B"] = count
  print("number of days: ", count)
  dashboard.at["Number of cases", "B"] = len(rawExpectedTimes)
  print("number of cases: ", len(rawExpectedTimes))
  dashboard.at["Original overtime frequency", "B"] = round(currentOvertimeCount / count, 2)
  print("current overtime frequency: %.0f%%" % (100 * currentOvertimeCount / count))
  dashboard.at["Original undertime frequency", "B"] = round(currentUndertimeCount / count,
2)
  print("current undertime frequency: %.0f%%" % (100 * currentUndertimeCount / count))
  dashboard.at["Model overtime frequency", "B"] = round(solver.Value(overtimeCount) /
count, 2)
  print("model overtime frequency: %.0f%%" % (100 * solver.Value(overtimeCount) / count))
  dashboard.at["Model undertime frequency", "B"] = round(solver.Value(undertimeCount) /
  print("model undertime frequency: %.0f%%" % (100 * solver.Value(undertimeCount) /
count))
  # Output overtime minutes and overtime cost
  originalOverMinutes = 0
  modelOverMinutes = 0
  originalCost = 0
  modelCost = 0
  for day in days:
    if solver. Value(totalScheduledTime[day]) < actualTotalTime[day]:
       modelOverMinutes += actualTotalTime[day] - solver.Value(totalScheduledTime[day])
       modelCost += math.ceil((actualTotalTime[day] -
solver.Value(totalScheduledTime[day])) / overtimeBlockLength) * noOfNursesPerBlock *
overtimeSalary
    if expectedTotalTime[day] < actualTotalTime[day]:
       originalOverMinutes += actualTotalTime[day] - expectedTotalTime[day]
       originalCost += math.ceil((actualTotalTime[day] - expectedTotalTime[day]) /
overtimeBlockLength) * noOfNursesPerBlock * overtimeSalary
```

```
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  dashboard.at["Original Overtime Minutes Used", "B"] = originalOverMinutes
  print("Model overtime minutes used: ", modelOverMinutes)
  dashboard.at["Model Overtime Minutes Used", "B"] = modelOverMinutes
  print("Original overtime cost: ", originalCost)
  dashboard.at["Original Overtime Cost", "B"] = originalCost
  print("Model overtime cost: ", modelCost)
  dashboard.at["Model Overtime Cost", "B"] = modelCost
  print("\n")
  # Output original and machine learning scheduling times for each procedure
  dashboard.at["Procedure Type", "B"] = "Original Time"
  dashboard.at["Procedure Type", "C"] = "Machine Learning Time"
  for p in procedureTypes:
    print(p + ": " + "%d" % solver.Value(procedureSchedulingTimes[p]))
    dashboard.at[p, "B"] = originalBookTimes[p]
    dashboard.at[p, "C"] = solver.Value(procedureSchedulingTimes[p])
  # Output cases completed with model and OR minutes used by original and machine
learning methods
  totalNoCases = 0
  originalCases = 0
  modelCases = 0
  original Minutes = 0
  modelMinutes = 0
  totalMinutes = 0
  print("\n")
  for day in days:
    noOfCases = len(actualTimes[day])
    totalNoCases += noOfCases
    originalMinutes += actualTotalTime[day]
    modelMinutes += solver.Value(totalScheduledTime[day])
    ORTime = 450 - (noOfCases - 1) * 15
    totalMinutes += ORTime
    originalTime = (ORTime - actualTotalTime[day])
    modelTime = (ORTime - solver.Value(totalScheduledTime[day]))
    originalCases += noOfCases
    if originalTime < 0:
       for i in reversed(range(len(actualTimes[day]))):
         originalTime += actualTimes[day][i]
```

```
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         originalCases -= 1
         if originalTime > 0:
            break
    modelCases += noOfCases
    if modelTime < 0:
       for i in reversed(range(len(actualTimes[day]))):
         modelTime += actualTimes[day][i]
         modelCases -= 1
         if modelTime > 0:
            break
  print("Cases achieved with machine learning model: %.0f%%" % (100 * modelCases /
totalNoCases))
  dashboard.at["Model cases achieved", "B"] = round(modelCases / totalNoCases, 2)
  print("OR minutes used with original model: %.0f%%" % (100 * originalMinutes /
totalMinutes))
  dashboard.at["Original OR minutes used", "B"] = round(originalMinutes / totalMinutes, 2)
  print("OR minutes used with machine learning model: %.0f%%" % (100 * modelMinutes /
totalMinutes))
  dashboard.at["Model OR minutes used", "B"] = round(modelMinutes / totalMinutes, 2)
  dashboard.to_excel(r'' + excelOutputFile, index=False)
else:
  print("No feasible solution found.")
```

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Surgery Division 1 2017 - 2019

Surgery Division 1 2017 - 2019														
	Surgeon 1 155 847 99.00%		155 135		Surg	eon 3	Surg	eon 4	Surg	eon 5	Sur	geon 6	Surgeon 7	
Number of Days					176 733		154		1:	94	183		140	
Number of Cases							7	03	7:	53	(655	567	
Machine Learning Cases Achieved			95.6	67%	94.67%		91.67%		91.33%		93.00%		96.33%	
	Original	ML Model	Original	ML Model	Original	ML Model	Original	ML Model	Original	ML Model	Original	Machine Learning	Original	ML Model
Overtime Frequency	13.33%	21.33%	48.67%	20.67%	32.67%	21.67%	55.33%	28.00%	54.67%	22.33%	58.33%	25.00%	47.33%	27.67%
Undertime Frequency	74.00%	17.00%	31.00%	13.00%	56.67%	14.33%	35.33%	10.00%	30.00%	24.67%	27.33%	15.33%	40.33%	10.67%
Overtime Minutes Used	623	1586	2933	2127	2200	2825	3926	2525	4997	3303	5041	2525	3066	2757
Overtime Cost	\$9937.50	\$26250.00	\$42750.00	\$32437.50	\$33375.00	\$42000.00	\$56812.50	\$39187.50	\$72000.00	\$48562.50	\$73312.50	\$39750.00	\$44625.00	\$40312.50
Percentage of OR Minutes Used	75.00%	76.33%	71.67%	71.67%	73.67%	73.00%	88.33%	86.67%	81.67%	83.00%	76.67%	77.00%	76.67%	74.67%
Scheduling Times (mins)														
Procedure 1	55	56												
Procedure 2	60	61	60	71	52	59	88	114	74	86	68	63	74	66
Procedure 3			53	64										
Procedure 4									94	112			106	103
Procedure 5			86	64										
Procedure 6			102	96	78	78								
Procedure 7											157	143		
Procedure 8	139	125							205	262				
Procedure 9			170	176	173	143			174	160			169	154
Procedure 10	54	54	69	73	62	66	70	63	73	68	86	81	70	76
Procedure 11	50	37					55	56	65	70	65	57	46	37
Procedure 12									94	111				
Procedure 13	80	74												
Procedure 14	50	40	61	64	60	57	70	71	62	70	78	81	62	65
Procedure 15							35	37						
Procedure 16							58	72						
Procedure 17					31	24								
Procedure 18					31	24								
Procedure 19							48	58						
Procedure 20	58	60					92	91	96	100	100	109	78	80
Procedure 21			112	135	111	70								
Procedure 22			72	82			72	62						
Procedure 23	45	34									57	58	44	42
Procedure 24	45	36	65	47	44	51	61	59	51	59	53	54	48	44
Procedure 25											25	39		

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Procedure 26			37	35			46	46	37	33

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Surgery Division 2 2017 - 2019

Surgery Division 2 2017 - 2019																
Surgeon 1		geon 1	Surç	geon 2	Surg	eon 3	Surg	eon 4	Surç	geon 5	Surg	eon 6	Surg	jeon 7	Surg	eon 8
Number of Days	201		2	230	2	32	3	08	2	253	7	0	3	04	2	40
Number of Cases	,	946	758		758 552		1161		879		173		821		561	
Machine Learning Cases Achieved	99	9.00%	99.33%		99.33%		100.00%		98.67%		97.0	00%	100	.00%	95.00%	
	Original	ML Model	Original	ML Model												
Overtime Frequency	45.67%	29.00%	46.00%	27.67%	36.33%	25.00%	57.33%	38.00%	55.67%	31.33%	53.00%	29.00%	49.33%	34.67%	62.67%	19.67%
Undertime Frequency	33.67%	20.33%	32.67%	18.00%	45.00%	19.00%	19.33%	19.67%	31.67%	19.00%	33.00%	19.00%	30.00%	21.67%	22.33%	23.33%
Overtime Minutes Used	2121	1850	2481	2027	2379	2093	3449	2852	4738	3311	1626	986	3079	2965	7980	4558
Overtime Cost	\$35062.50	\$30562.50	\$41250.00	\$35812.50	\$38625.00	\$34312.50	\$60187.50	\$48562.50	\$72562.50	\$52312.50	\$23437.50	\$15562.50	\$53250.00	\$48750.00	\$113250.00	\$68250.00
Percentage of OR Minutes Used	80.67%	81.00%	81.33%	82.00%	58.33%	58.67%	62.00%	62.00%	77.33%	77.33%	61.00%	60.00%	59.33%	60.00%	59.67%	61.67%
Scheduling Times (mins)																
Procedure 1			115	117	124	108	76	77	87	80	110	118	91	102		
Procedure 2	151	121														
Procedure 3											132	55			129	119
Procedure 4	87	78														
Procedure 5	115	104														
Procedure 6					55	71	50	55			50	72	55	49		
Procedure 7															59	56
Procedure 8	94	93														
Procedure 9									33	40						
Procedure 10					190	163	142	120	131	130			142	133		
Procedure 11															133	186
Procedure 12			143	128												
Procedure 13	116	111													120	171
Procedure 14			113	114												
Procedure 15					137	137	94	94	123	130			107	100		
Procedure 16								•					118	121		
Procedure 17			145	138												
Procedure 18	91	98	133	125												
Procedure 19	Ţ.		, 00	0					113	115						
Procedure 20									1.0	110					118	118
Procedure 21			105	104											110	110
Procedure 22	132	109	103	104												
Procedure 23	132	109							37	40			40	58		
Procedure 24			114	114					37	40	128	127	40	30		
Procedure 25			114	114	88	125					120	127				
Procedure 26					82	81					92	75			99	108
Procedure 27					02	01	103	90			92	75			99	108
Procedure 28							103	80			90	400			00	450
			100	400							90	122			92	150
Procedure 29	400	400	106	122	400	400	444	404			444	00				
Procedure 30	106	102	117	113	138	122	111	101			111	96				
Procedure 31											85	115				
Procedure 32															119	120
Procedure 33									152	162						
Procedure 34	36	35	43	48	50	49	32	36	54	60	44	92	38	40	72	95
Procedure 35					93	98	95	82	90	139	75	127	105	75	108	126

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Procedure 36						130	97	139	125		137	144	
Procedure 37	54	52		60	50	85	93				47	51	